NPS-ME-93-004



NAVAL POSTGRADUATE SCHOOL Monterey, California

AD-A269 928



WAVELET TRANSFORM FOR TIME-FREQUENCY ANALYSIS OF VIBRATIONAL SIGNATURE AND ITS APPLICATION

by

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August 17, 1993

Approved for Public Release; Distribution Unlimited

Prepared for: Naval Postgraduate School

Monterey, CA 93943

Naval Seas Systems Command

PMS390

Washington, D.C.





Naval Postgraduate School Monterey, California

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This report was prepared in conjunction with research conducted for and funded by both the Naval Postgraduate School and the Naval Sea Systems Command, PMS390, Washington D.C.

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REPORT DOCUMENTATION PAGE

FormApproved OMB No. 0704-0188

Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instruction, searching emissing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden to Washington Headquaters Services, Directorate for information Operations and Reports, 1215 Jefferson David History Suits 1204 Avincton VA 22202-2432, and to the Office of Management and Reports Processor Selection Processor Selecti

collection of information, including suggestions for reducir Davis Highway, Suite 1204, Arlington, VA 22202-4302, an	og this burden to Washington Headquater of to the Office of Management and Budge	Services, Directorate for it. L. Paperwork Reduction Pri	nformation Operations and Reports, 1215 Jefferson operi/0704-0188), Washington, DC 20503	
	2. REPORT DATE		REPORT TYPE AND DATES COVERED	
	17 Aug. 93		1 Mar 93 - 16 Aug 93	
4. TITLE AND SUBTITLE			5. FUNDING NUMBERS	
WAVELET TRANSFORM FOR TIME-FREQUENCY ANALYSIS OF THE VIBRATIONAL SIGNATURE AND ITS APPLICATION			N0002493WR02460	
6. AUTHOR(S)	MESG1			
Jae-Jin Jeon and Youn	g S. Shin			
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES) Naval Postgraduate School Monterey, CA 93943-5000			8. PERFORMING ORGANIZATION REPORT NUMBER	
			3777 AP 40 404	
			NPS-ME-93-004	
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES)			10. SPONSORING/MONITORING	
Naval Postgraduate School	AGENCY REPORT NUMBER			
Naval Sea Systems Comm	and, PMS 390			
Washington, DC 20362-510	01			
11. SUPPLEMENTARY NOTES				
The views expressed are to position of DOD or US Go		nd do not refl	ect the official policy or	
12a. DISTRIBUTION/AVAILABILITY S	TATEMENT		12b. DISTRIBUTION CODE	
Approved for public release	se:			
Distribution is unlimited.				

13. ABSTRACT (Maximum 200 words)

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14. SUBJECT TERMS Wavelet Transform, Gaussian Wavelet, Vibration Signature Analysis, Time-Frequency Domain			15. NUMBER OF PAGES 64
			16. PRICE CODE
17. SECURITY CLASSIFICATION OF REPORT UNCLASSIFIED	18. SECURITY CLASSIFICATION OF THIS PAGE UNCLASSIFIED	19. SECURIT: CLASSIFICATION OF ABSTRACT UNCLASSIFIED	20. LIMITATION OF ABSTRACT SAR

NSN 7540-01-280-5500

Standard Form 298 (Rev 2-89)

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ABSTRACT

Wavelet transform is applied to the analysis of vibration signatures in order to verify the ability of the detection of abnormal condition. It can well describe the dynamics of the signal's spectral composition of a non-stationary and stationary signal to be measured and presented in the form of 3-D time-frequency map. Although wavelet has been developed over about ten years in the mathematics and physics, its engineering applications is a first stage. The objective of this report outlines the definition of the wavelet transform and is to discuss the properties of the wavelet transform as new tool for the vibration analysis, and then demonstrates how it may be applied to the machinery condition monitoring.

I. INTRODUCTION

Wavelets are a very popular topic of the signal processing and applied mathematics. In the last ten years, an interest in them has grown at an fast rate in signal and numerical analysis [Beylkin, Coifman and Rokhlin, 1991, Heil, 1990 and Resnikoff and Burrus, 1990]. Wavelet analysis appears to new subject for the time-frequency analysis of the vibrational signatures. Traditional spectral analysis provides spectral values which are independent of time. It is assumed to be ergodic and stationary signal with

time. However the signal associated with most vibrational phenomena are in general time varying, which means that their characteristics change with time and they have various features in different time frames. For example, the vibration during the start-up of an engine or pump is non-stationary, the sound pressure generated from speaker is nonstationary, and so on. In case of the signal containing some transient or nonstationary conditions, the traditional approach in signal analysis fails to describe the dynamics of the signal's frequency components changes. Changes in the condition of a component such as a gear can be expected to cause some change in the vibration generated by mechanical system. Very little damage detection can be performed using the vibration signal directly from the system because the small changes generated by early damage may be masked by the normal vibration of the system.

Two methods of signal analysis for nonstationary application are commonly used in time-frequency domain. The windowed Fourier transform, otherwise so called short time Fourier transform(STFT), has a short time window of a fixed size centered at time t as figure 1(a). The windowed Fourier transform is given as follows

$$F(\omega,t) = \int g(\tau - t) e^{-i\omega\tau} s(\tau) d\tau$$
 (1)

where $F(\omega,t)$ is the windowed Fourier transform, g(t) window function and s(t) time signal. The range of integration is from $-\infty$ to ∞ . If the length of the window is time duration T, the resolution of time frequency domain depends on T. Its frequency bandwidth or frequency resolution is approximately ν T. Therefore this method have the limitation of resolution in both time and frequency domain simultaneously.

The second method, often called Wigner distribution method, is based on the instantaneous power spectra defined as following equation (2)

$$w(\omega,t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} s(t-\tau/2) s(t+\tau/2) e^{-i\omega\tau} d\tau$$
 (2)

where $w(\omega,t)$ is Wigner distribution function. Equation (2) is called the Wigner distribution of s(t) in figure 1(b). We discussed well at references [Jeon and Shin (1993) and Shin, Jeon and Spooner (1993)] about the characteristics of Wigner-Ville distribution. For a nostationary signal analysis, spectrogram is commonly used, which is based on the assumption that it is a collection of a short duration stationary signal.

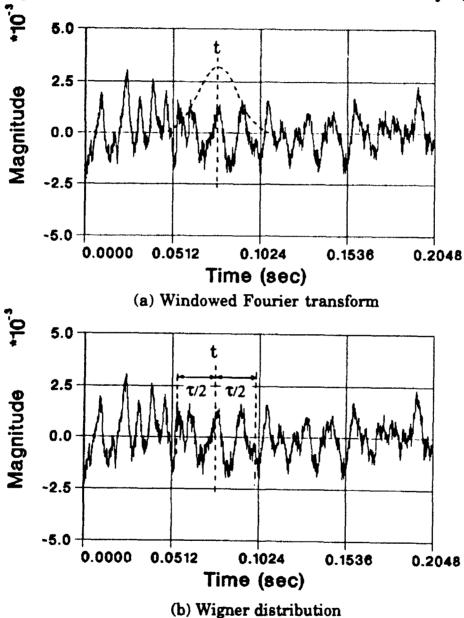


Figure 1. Calculation of the windowed Fourier transform and instantaneous spectral density(Wigner distribution) of a vibration signal.

A major drawback of this approach is that the frequency resolution is directly affected by the duration of short stationary time, which subsequently determines the time resolution. The frequency and time resolution of the Wigner distribution are not determined by the short duration but rather determined by the selection of desired resolution of the signal itself, but may not be appropriate for signals containing patterns at both large and very small scales.

The windowed Fourier transform is well portray the characteristics of signals in which all of the patterns appear at approximately the same scale, but may not be appropriate for signals containing patterns at both large and small scales because of the time fixed window size. multifrequency channel decomposition, which are an intermediate between a time and a Fourier representation, have found many applications in signal and image processing [Mallat, 1989]. Much recent research has been focused on this domain with the modeling of a new decomposition called the wavelet transform, which is presented signal by summation of family of functions which are the dilations and translations of a unique function called a wavelet. Instead of portraying a signal into harmonic functions ($e^{i\omega t}$ in Fourier transform), the signal is presented into a series of orthogonal basis functions of finite length. Each wavelet is located at a different position on the time axis. At the finest scale, wavelets may be very short indeed; at a coarse scale, they may be very long. Alternatively very small disturbances in a record of machinery vibration can be easily characterized from a wavelet 3-D or 2-D map in which the mean-square value of the time record is shown over wavelet scale and position.

One important property of a wavelet transform is its ability to characterize easily the local regularity of a function. Simply by a change of the scale parameter(dilation) in the wavelet transform, many scales of local structure can be described by a distribution in the time-scale plane. Wang and McFadden (1993) introduced the advantage for examining the vibration signal generated by a gear and D. E. Newland (1993) well investigated the properties of the wavelet as a new tool for the analysis of vibration records.

This report outlines the definition of the wavelet transform, compare with the advantages and the disadvantages of wavelet and pseudo Wigner-Ville distribution in time-frequency domain analysis, and then demonstrates how it may be applied to analysis of the vibration signals for the machinery condition monitoring.

II. DEFINITION OF WAVELET TRANSFORM

To overcome the limitation of the fixed resolution of the windowed Fourier transform in the time and frequency domains by decomposing the signal s(t) into a family of functions which are the translation and dilation of an unique function $\psi(t)$, defined the continuous wavelet transform as

$$W(a,b) = \frac{1}{\sqrt{a}} \int_{-\infty}^{\infty} \psi(\frac{t-b}{a}) s(t) dt$$
 (3)

where W(a,b) is wavelet transform, ψ is an analyzing wavelet, a represents a time dilation, b a time translation, and bar for complex conjugate. The normalization factor $1/\sqrt{a}$ is perhaps most effectively visualized as endowing $|W(a,b)|^2$ with unit of power/Hertz [Shensa, 1992].

We consider the space $L^2(\mathbf{R})$ of measurable function ψ , defined on the real line \mathbf{R} ($\mathbf{R} := (-\infty, \infty)$), certain weak 'admissibility' conditions are usually required on $\psi(t)$ [Shensa, 1992];

$$\int_{-\infty}^{\infty} \frac{|\hat{\psi}(\omega)|^2}{|\omega|} d\omega < \infty \tag{4}$$

where $\hat{\psi}(\omega)$ is the Fourier transform of $\psi(t)$. They ensure that the transformation is a bounded invertible operator in appropriate space [Daubechies, 1988]. If $\hat{\psi}(\omega)$ is differentiable, then it suffices that ψ be zero mean, that is,

$$\int_{-\infty}^{\infty} \psi(t) dt = 0$$
 (5)

for equation (4) to be satisfied. In particular, since the local average values of every function in $L^2(\mathbf{R})$ must 'decay' to zero at $\pm \infty$, the sinusoidal(wave) functions $e^{i\omega t}$ (basis of Fourier transform) do not belong to $L^2(\mathbf{R})$. Fourier series representation of any functions is in $L^2(0,2\pi)$. In fact, if it looks for

wavelets that generate $L^2(\mathbf{R})$, these wavelets should decay to zero at $\pm \infty$; and for all practical purposes, the decay should be very fast [Chui, 1992].

In signal processing, the significance of equation (3) is well understood by comparing it to the windowed Fourier transform (or short-time Fourier transform):

$$F(\omega,b) = \int_{-\infty}^{\infty} g(t-b) e^{-i\omega t} s(t) dt.$$
 (6)

Thus, to obtain $F(\omega, b)$, one multiplies the signal by an appropriate window g(t) (such as Gaussian) centered at time b and then takes the Fourier In mathematical forms, equation (6) is an expansion of the transform. signal in terms of family of functions g(t-b)eiot, which are generated from a single function g(t) through translations b in time and translations ω in In contrast, the wavelet transform of equation (3) is an expansion in function $\psi((t-b)/a)$ generated by translation b and dilation a in time. Thus, the continuous wavelet transform is similar to windowed Fourier transform with a different window size for each frequency. The important facts of this is that, while the basis functions in equation (6) have the same time and frequency resolution at all points of the transform plane, those of wavelet transform have the time resolution which decrease with increasing a and the frequency resolution which increase with decreasing a width adapted to their frequency components: at high frequency ψ are very narrow, while at low frequency ψ are much broader. As a results, the wavelet transform is better than the windowed Fourier transform to analyze on very small disturbance, i.e., high frequency phenomena. property can be a best advantage in signal processing since high frequency characteristics are generally highly localized in time whereas slowly varying signals require good low frequency resolution [Shensa, 1992]. Figure 2 shows the typical shapes of windowed Fourier transform functions and wavelet.

The wavelet transform means that signal s(t) is characterized by decomposition into a set of wavelet family with series of different frequency

bandwidth. For the decomposition of the signal s(t) defined on real line, it is necessary to shift ψ along R. Let Z denote the set of integers;

$$Z = \{ \dots -1, 0, 1, \dots \}.$$

The simplest way for ψ to cover all of R is to consider all the integral shift of ψ ,

$$\psi(t-k), \quad k \in \mathbb{Z}. \tag{7}$$

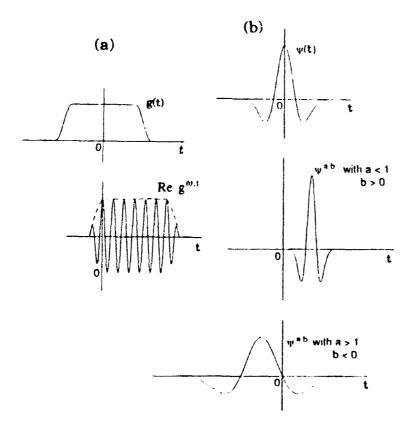


Figure 2. The typical shapes of (a) windowed Fourier transform function g(t), (b) wavelet $\psi^{a,b}$, $\psi(t) = (1-t^2) e^{-t^2/2}$ [Daubechies, 1992].

Next, as in Fourier transform, it must be also considered wavelets with different frequencies. It is considered wavelets with frequencies partitioned into consecutive 'octaves' (or frequency bands). For computational efficiency, it will be used integral power of 2 for frequency partitioning, that is, the small wavelets is considered as follows

$$\psi(2^{j}t - k), \qquad j,k \in \mathbb{Z}. \tag{8}$$

From the equation (3), $\psi(2^jt-k)$ is obtained from the wavelet function $\psi(t)$ by dilation of $1/2^j$ and translation of $k/2^j$. An important particular case of the discrete wavelet transform which was found is that some wavelets $\psi(t)$ exist such that $\sqrt{2^j} \psi(2^j(t-2^{-j}k))_{(j,k)\in \mathbb{Z}}$ is an orthonormal basis of $L^2(\mathbb{R})$ [Mallat, 1989].

As originally proposed by Morlet et al. (1982), ψ was a modulated Gaussian

$$\psi(t) = e^{i\omega_0 t} e^{-t^2/2}$$
 (9)

and this function is selected to analysis the vibration of gear box for signal processing applications [Wang and McFadden, 1993]. The example of a shape for the modulated Gaussian wavelet is shown in figure 3. The Fourier transform of the first wavelet family $\psi(t/a)$, i.e., no translation, is

$$\hat{\Psi}(a\omega) = a e^{-(\omega - \omega_0/a)^2 a^2/2} \tag{10}$$

which has analysis frequency ω_0/a . ω_0/a is a simple frequency parameter which determines the analyzing wavelet. We can easily see that equation (9) satisfies the admissibility condition equation (4). The analyzing bandwidth of the wavelet is proportional to 1/a, thus having a constant relative bandwidth(BW), that is, $BW/(\omega_0/a) = constant$. This feature is also reflected in the narrow time window at higher frequency(i.e., at smaller a). In general, the function $\psi(t)$ is selected by its time and frequency localization properties [Daubechies, 1990].

The scale change may be performed by substituting $a = 2^{-j}$ for the computation efficiency. In this case the wavelet family is $\sqrt{2^j} \psi(2^j t)$, and the definition of the wavelet transform becomes

$$W(2^{j}, b) = \frac{1}{\sqrt{2^{j}}} \int_{-\infty}^{\infty} \psi(\frac{t-b}{2^{j}}) s(t) dt$$
 (11)

In this report, the unique function $\psi(t)$ can be selected to be a well-behaved modulated Gaussian function, given by equation (9).

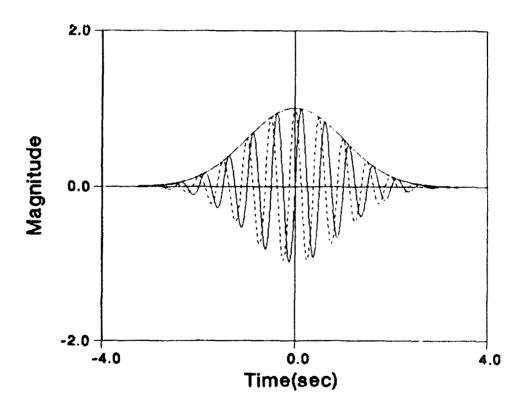


Figure 3. Example of modulated Gaussian wavelet. $(\psi(t) = e^{i\omega_0 t} e^{-t^2/2}, \omega_0 = 2\pi f_0, f_0 = 2 \text{ Hz})$

III. TIME-FREQUENCY ANALYSIS

Suppose that ψ is any basic wavelet such that both ψ and its Fourier transform $\hat{\psi}$ are window functions which have centers and half widths of time and frequency domain given by t^* , ω^* , Δt , $\Delta \omega$, respectively. Then the wavelet transform of an analog signal s(t) is given as follows.

$$W(a,b) = |a|^{-1/2} \int_{-\infty}^{\infty} s(t) \overline{\psi(\frac{t-b}{a})} dt$$
 (12)

Equation (12) localizes the signal with a time window

$$[b + at^* - a\Delta t, b + at^* + a\Delta t],$$

where the center of the window is at $b + at^*$ and the width is given by $2a\Delta t$. This is called time localization in signal analysis.

On the other hand, let set the Fourier transform of ψ

$$\eta(\omega) = \hat{\psi}(\omega + \omega^*), \tag{13}$$

where η is the Fourier transform of ψ , then η is also a window function with center at ω^* and width by $\Delta \omega$, and by Parseval identity, the wavelet transform in equation (12) becomes [Chui, 1992]

$$W(a,b) = \frac{a|a|^{-1/2}}{2\pi} \int_{-\infty}^{\infty} \hat{s}(\omega) e^{ib\omega} \overline{\eta(a(\omega - \frac{\omega^*}{a}) d\omega}$$
 (14)

where the phase shift of $e^{ib\omega}$ is determined by translation along time axis. Equation (14) is also localized information of spectrum $\hat{s}(\omega)$ of the signal s(t) with frequency window

$$\left[\frac{\omega^*}{a} - \frac{1}{a}\Delta\omega, \frac{\omega^*}{a} + \frac{1}{a}\Delta\omega\right],$$

where the center of window is at ω^*/a and width is given by $2\Delta\omega/a$. This is called frequency localization.

From equation (12) and (14), time-frequency window of wavelet transform is as follows.

$$[b + at^* - a\Delta t, b + at^* + a\Delta t] \times \left[\frac{\omega^*}{a} - \frac{1}{a}\Delta\omega, \frac{\omega^*}{a} + \frac{1}{a}\Delta\omega\right]$$
 (15)

The covered area by time-frequency window is the multiplication of time and frequency bandwidth around the center of window. The time-frequency window is shown figure 4. Eventually it is considered positive frequencies, i.e., a > 0, the basic wavelet ψ may be chosen that the center ω^* of $\hat{\psi}$ is a positive number. The ratio of the center frequency to the width of frequency band is given by

$$\frac{\omega^*/a}{2\Delta\omega/a} = \frac{\omega^*}{2\Delta\omega} \tag{16}$$

which is independent of the location of the center frequency. This is called constant percentage band width analysis or constant-Q frequency analysis. In this report, the octave band is used for the analysis of vibration signal. The frequency window along the frequency axis narrows for large center frequency ω^*/a and widens for small one and the time window is opposite to frequency window. The area of the window is a constant, given by $4\Delta t\Delta\omega$.

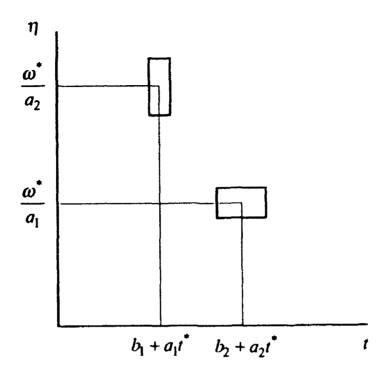


Figure 4. Time-frequency windows, $a_1 > a_2$.

IV. DISCRETE WAVELET TRANSFORM

In the continuous wavelet, the family is considered

$$\psi^{a,b}(t) = |a|^{-1/2} \psi(\frac{t-b}{a})$$
 (17)

where $b \in \mathbb{R}$, $a \in \mathbb{R}_+$ with $a \neq 0$, and ψ is admissible. \mathbb{R} denotes the real line and R+ denotes the positive real line. It is considered with discrete values for a and b. For the discretization of the dilation parameter, we select $a = a_0^m$, where $m \in \mathbb{Z}$, and the dilation step $a_0 \neq 1$ is fixed. convenience, it assume $a_0 > 1$. If $a_0 = 1$, the wavelet transform may be similar to windowed Fourier transform. For m = 0, it seems natural as well to dicretize b by taking only the integer multiples of one fixed b_0 , where b_0 is appropriately chosen so that the $\psi(t - nb_0)$ cover the whole line. We arbitrarily fix $b_0 > 0$ in this report. For the different values of m, the width of $a_0^{-m/2} \psi(a_0^{-m} t)$ is a_0^m times the width of $\psi(t)$ defined at section III, so that the choice $b = nb_0a_0^m$ will ensure that the discretized wavelets at level m cover the line in the same way that $\psi(t - nb_0)$ do. Thus it is selected, $a = a_0^m$, $b = nb_0 a_0^m$, where m,n range over **Z**, and $a_0 > 1$, $b_0 > 0$ are fixed; the appropriate choices for a_0 and b_0 depend on the wavelet ψ The discrete form of equation (17) is and the characteristics of signal. given as following equation [Daubechies, 1992]

$$\psi_{m,n}(t) = a_0^{-m/2} \psi(\frac{t - nb_0 a_0^m}{a_0^m})$$

$$= a_0^{-m/2} \psi(a_0^{-m}t - nb_0)$$
(18)

For the computation efficiency, we assume that $a = 2^m$, that is, $a_0 = 2$, where m is termed the octave of the transform. This means that the

frequency resolution of wavelet has a octave band. The integral equation (3) yields a wavelet series as following equation by using equation (18).

$$W(2^{m}, nb_{0}) = \frac{1}{\sqrt{2^{m}}} \int_{-\infty}^{\infty} \overline{\psi(\frac{t - nb_{0}}{2^{m}})} s(t) dt$$
 (19)

At the discrete wavelet transform, the finite energy for the wavelet transform is not equivalent to finite energy for the wavelet series. It depends on the sampling grid as well as the function $\psi(t)$. In addition, it often take b to be a multiple of a.

W(2^m, n2^m) =
$$\frac{1}{\sqrt{2^m}} \int_{-\infty}^{\infty} \psi(\frac{t}{2^m} - n) s(t) dt$$
 (20)

A logical step in applying the theory to discrete signal is to discretize the integral in equation (20) as follows.

$$W(2^{m}, n2^{m}) = \frac{1}{\sqrt{2^{m}}} \sum_{k} \overline{\psi(\frac{k}{2^{m}} - n)} s(k)$$
 (21)

Octave m is only output every 2^m samples. In this form the resulting algorithm will not be translation invariant [Mallat, 1982]. The discrete wavelet transform is highly not invariant under translations. In practice one does not use an infinite number of scales, but cuts off very low and very high frequencies.

V. EXAMPLES AND DISCUSSIONS

A signature generated by machinery involves many informations about its operating condition. It can be obtained the information about the operating condition of machinery by applying the analysis tools for the vibration records. Wavelet transform is a new tool that is particularly suited for time-frequency analysis of nonstationary or stationary signals. There are many advantages of using wavelet transform for both steady and transient signals. We will discuss the performance of the wavelet transform by using simple example and compare with pseudo Wigner-Ville distribution(PWVD) in time-frequency domain analysis.

Before showing some examples, it is necessary to discuss how best to describe the results. We have found that 3-D map and 2-D map of wavelet transform are a useful presentation for many applications. The square of the amplitude in equation (21) has the unit power/Hz. The distribution of the amplitude square over the individual wavelet and position can now be seen as figure 5. If the length of sampled data is shorter than the wavelet size, the distribution at lower wavelet level, i.e., low frequency, has the value at only one position.

In order to describe the results of wavelet transform, we use the 3-D and 2-D(for the complicated signal) graphics. And for graphic, the results of that is distributed and reduced to 256(3-D) or 512(2-D) data point along the time axis. Frequency axis is a log scale (octave scale or wavelet level) and time axis is a linear scale in figures of wavelet transform.

A. Harmonic wave with stepwise frequency changes

Figure 6 shows (a) the pure sine wave with stepwise frequency changes 500 Hz, 250 Hz and 100 Hz, (b) its PWVD and (c) the wavelet transform. The wavelet transform and PWVD well represent the time delay and the

frequency components of signal. The wavelet transform is a result with frequency partitioned into consecutive octaves for computational efficiency. Then the magnitude of 100 Hz is dispersed. But the wavelet transform clearly describes the time delay. From these figures, we can see that the PWVD has the higher resolution than the wavelet transform in frequency line. However the computation time of PWVD is extremely higher than the wavelet transform. Figure 7 shows the wavelet transform of the sine wave with 500 Hz in time from 0.085 sec to 0.17 sec. the wavelet transform well represents the time delay and the frequency band of the signal.

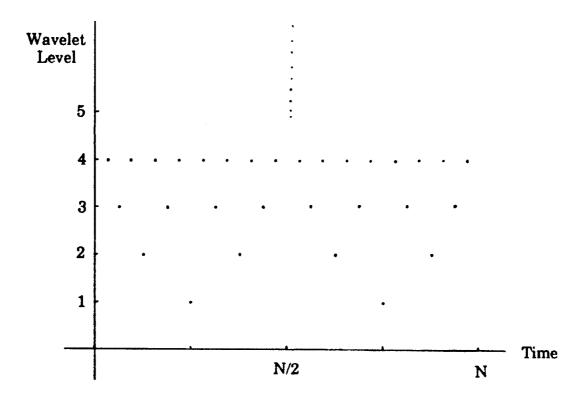
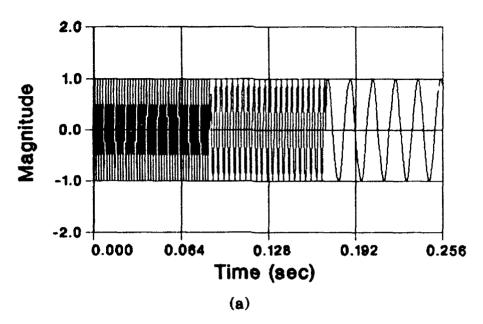
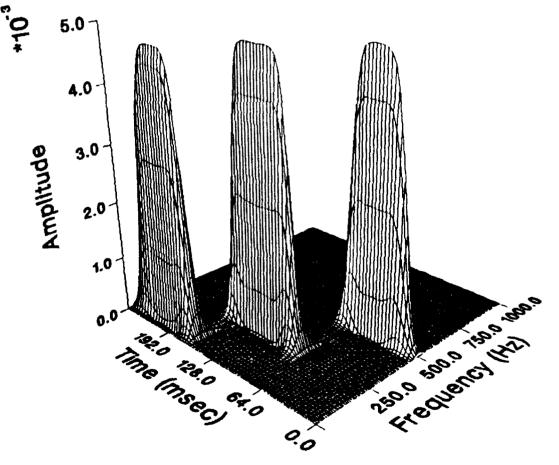


Figure 5. The lattice of time-frequency localization of wavelet transform
(N = Number of data points)





(b) Fig.6 (continued) 18

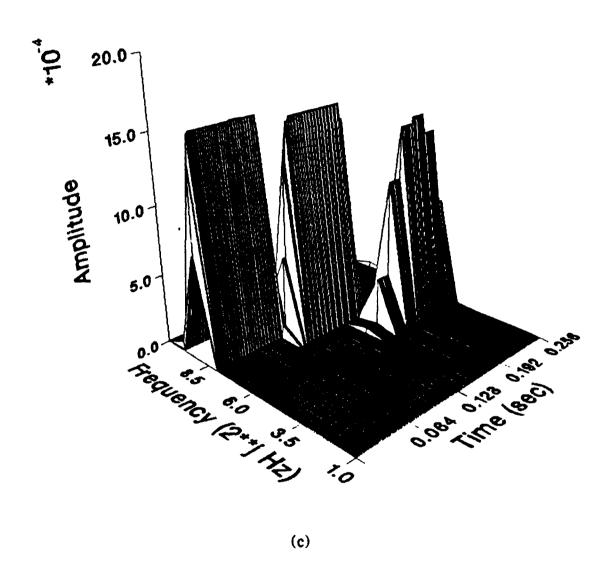


Figure 6. Time-frequency localization of PWVD and wavelet transform: (a) signal s(t), (b) its PWVD and (c) its wavelet transform (f_8 =2000 Hz, N=512).

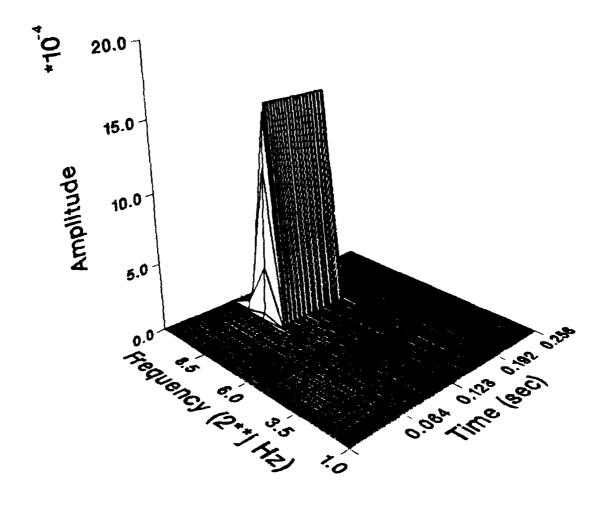
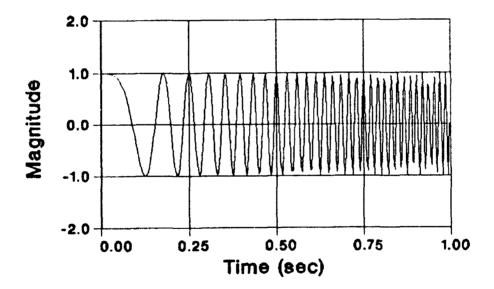


Figure 7. Wavelet transform for step sine wave (f = 500 Hz); f_S = 2000 Hz, N=512.

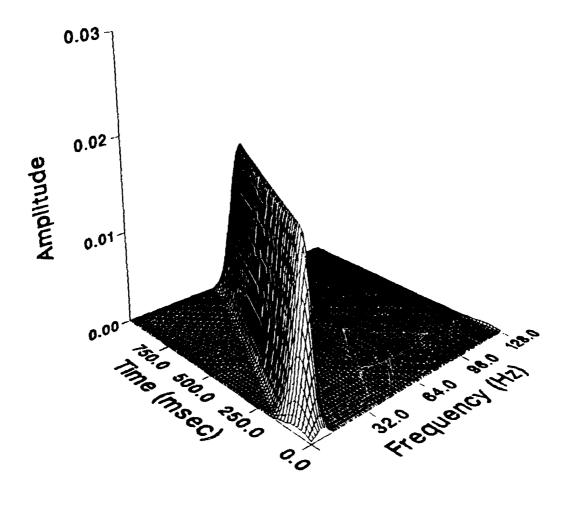
B. Swept harmonic wave

The effect of sweep rate on PWVD was well investigated at Jeon and Shin (1993), and Shin, Jeon and Spooner (1993). Figure 8. shows (a) the sweept cosine wave with the sweep rate 32 Hz/sec, (b) its PWVD and (c) its wavelet transform. From this figures, we can see that PWVD is a useful tool for analysis of the signal with fast frequency change in time. However if the records of signal is longer, the computation time may be much needed. The result of the wavelet transform does not clearly represents the sweep condition but well describes the change of frequency range with time.



(a)

Fig.8 (continued)



(b)

Fig.8 (continued)

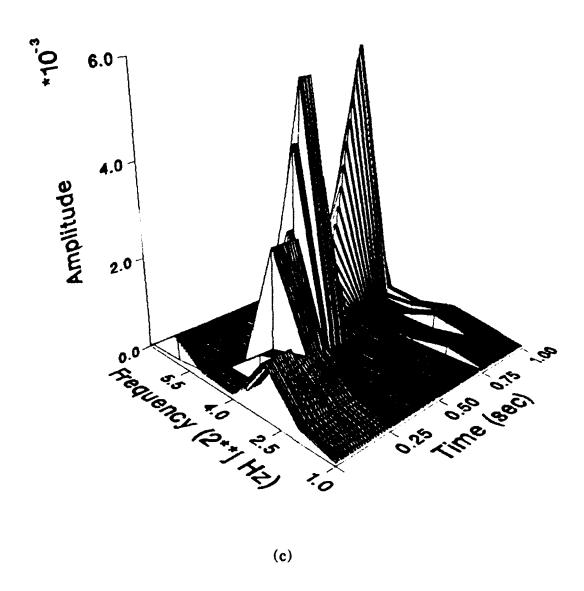


Figure 8. Time-frequency localization of the PWVD and wavelet transform: (a) signal $s(t) = \cos{(2\pi \ 32 \ t^2)}$, (b) its PWVD and (c) its wavelet transform ($f_S = 256 \ Hz$, N = 256).

C. Harmonic wave with glitches

The interesting phenomena on the signal with an abnormal component as a fault were investigated. Figure 9 shows (a) the harmonic wave with glitch at a small region, (b) is PWVD and (c) its wavelet transform. It can be seen that both PWVD and wavelet transform of the signal figure 9(a) well represents the location of each glitch and its frequency components. Figure 10 is the result of wavelet transform in case of sampling frequency From these figures, it can be clearly seen that the wavelet transform is very useful tool in the analysis of the signal required higher time resolution. Figure 9(c) shows the glitch components more clearly than PWVD because the wavelet transform has the very narrow time window in high frequency region. This characteristic of the wavelet transform is useful to detect the fault or glitch although the fault is small and to monitor the condition on any vibrational machinery under the steady operation condition. Also the wavelet transform is more effective for the analysis of signal which the time record length is long, since the sweep along the frequency line is octave step.

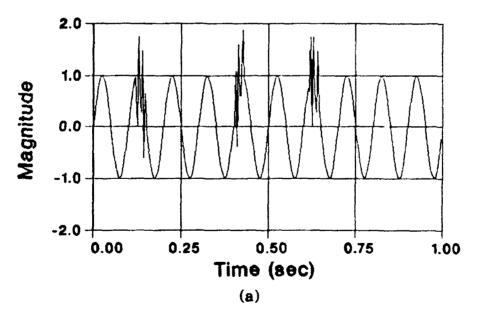
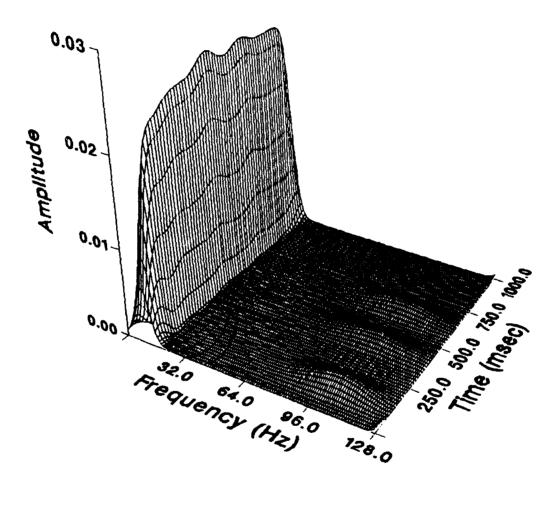


Fig.9 (continued)



(b)

Fig.9 (continued)

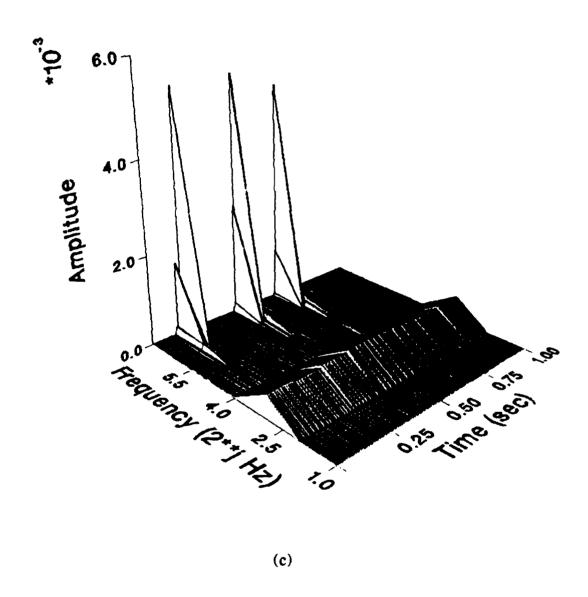


Figure 9. Time-frequency localization of PWVD and wavelet transform: (a) the signal s(t) [Jeon and Shin, 1993], (b) its PWVD and (c) its wavelet transform ($f_s = 256 \text{ Hz}$, N = 256).

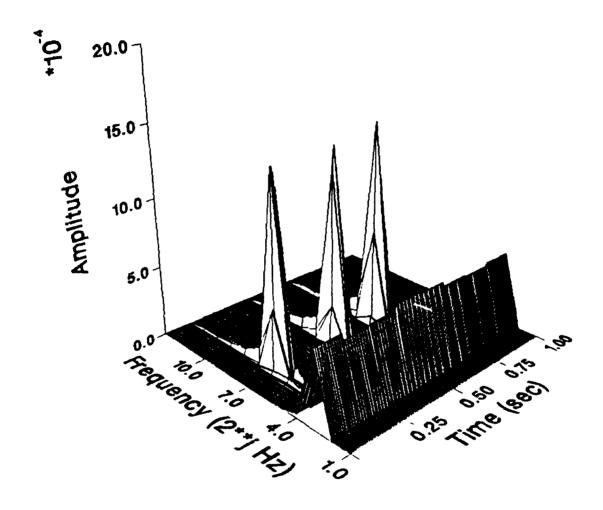


Figure 10. Time-frequency localization of wavelet transform for the signal Fig. 9(a) ($f_S = 8192 \text{ Hz}$, N = 8192).

D. Harmonic wave with pulse

Figure 11 illustrates about the signal including small changes generated by early damage. In practice, this signal is not given by this continuous expression, but by samples, and adding a δ -function is then approximated by adding a constant to one sample only. The example signal is generated by following equation.

$$s(t) = \sin(2\pi \ 100 \ t) + \sin(2\pi \ 500 \ t) + 1.5 \ \delta(t-0.049) + 1.5 \ \delta(t-0.061)$$
 (22)

From this figure, we can see that the wavelet transform has the great advantage for the analysis of the signature including the small disturbance. PWVD does not give the exact information about time delay of pulse but well represents about the frequency components of main signatures. The wavelet transform does not describe the magnitude of the main frequency components but well represents the time delay of pulse and is obtained the result by very short computation time. From this example, the wavelet transform is very useful tool to detect the fault although that is very small region on time axis.

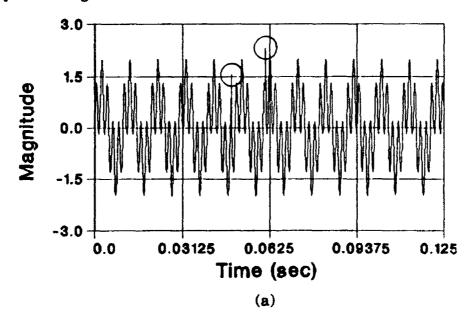
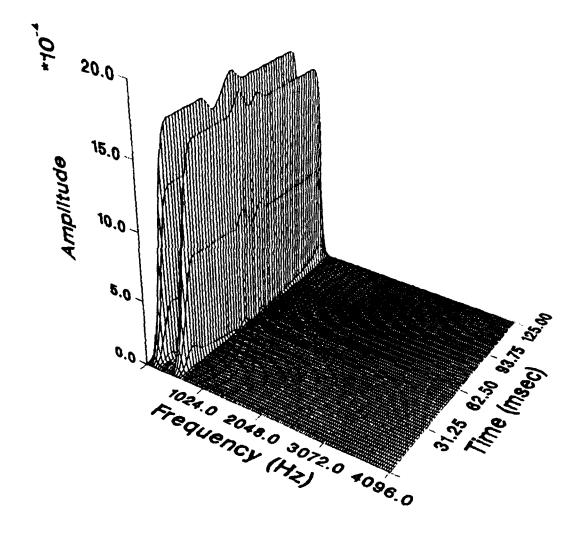


Fig.11 (continued)



(b)

Fig.11 (continued)

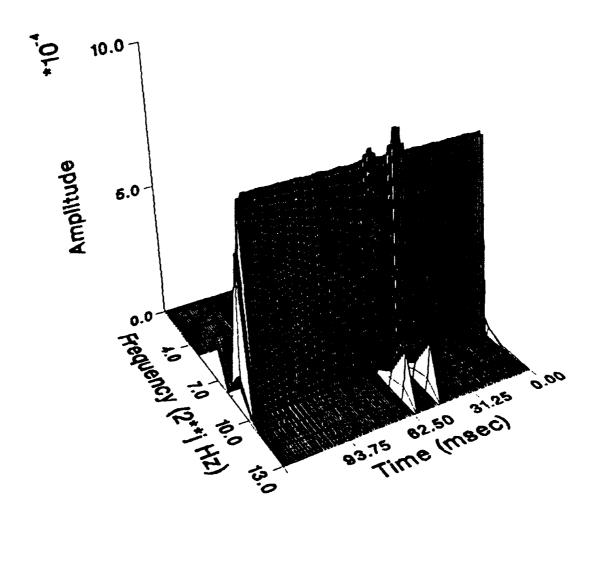


Figure 11. Time-frequency localization of PWVD and wavelet transform: (a) the signal s(t), (b) its PWVD and (c) its wavelet transform ($f_S = 8192 \text{ Hz}$, N = 1024)

(c)

E. Actual pump signal

The signal of actual pump was measured at the steady state speed without and with abnormal condition. Figure 12 show the time signal pattern for each condition, and figures 13 and 14 show the results of wavelet transform by using 3-D or 2-D graphics. Also figure 15 are the results of pseudo Wigner-Ville distribution. These figures show a very interesting results.

From these figures, we can easily find the abnormal condition. At 13th frequency band of figure 13(a) and (b), the results of wavelet transform obviously show the different condition and pattern for each case. And also at 8th frequency band, the small changes of patterns can be seen. Figure 14(a) and (b) well represent the operation condition although the shape is more complicate and we can see the abnormal state of pump.

In this case, if one wavelet to have 13th frequency band is used, it gives good results for diagnosis and vibration condition monitoring as very short computation time. Figure 15 are PWVD. Also PWVD well represents the abnormal condition but the computation time is very long than that of wavelet transform. In the case of wavelet transform, it is possible to independently compute for each wavelet level different from PWVD. The difference of computation time for the wavelet transform and PWVD is about 100 times for the number of sample data N=2048 in the calculation of a whole plane. At VAX3520, the computation time is 18 seconds for wavelet transform and about 30 minutes for PWVD.

Especially the wavelet transform may be very useful to detect the small disturbance over long record length and to analyze the signals which has a long time duration and intermittent abnormal condition such as non-rotating machinery. The advantage of the Wigner-Ville distribution is that, unlike the wavelet transform or the windowed Fourier transform, it does not introduce a reference function(such as wavelet or window function in Eq.(3) and (1)) against which the signal has to be integrated and the short

time signal. The disadvantage is that the signal enters in Wigner-Ville distribution in a quadratic rather than linear way, which causes many interference phenomena as shown in references Jeon and Shin (1993), and Shin, Jeon and Spooner (1993). Wigner-Ville distribution may be useful in some application for signals which have a very short time duration.

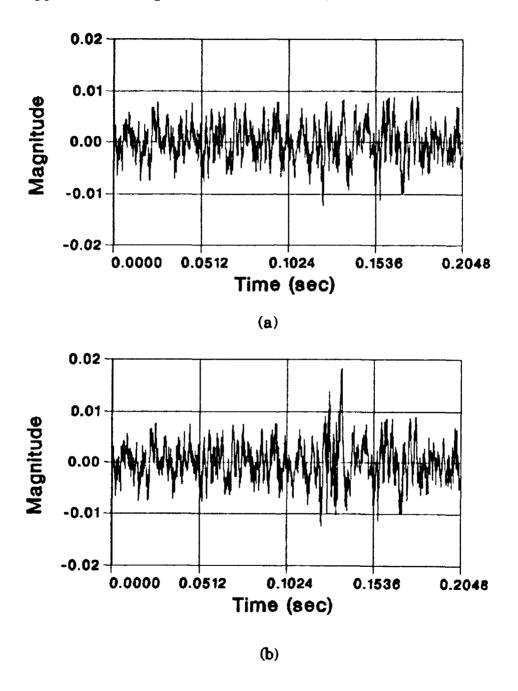
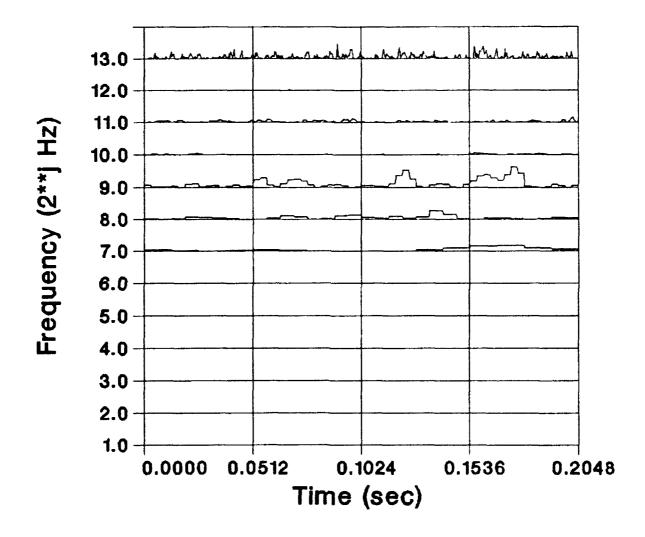
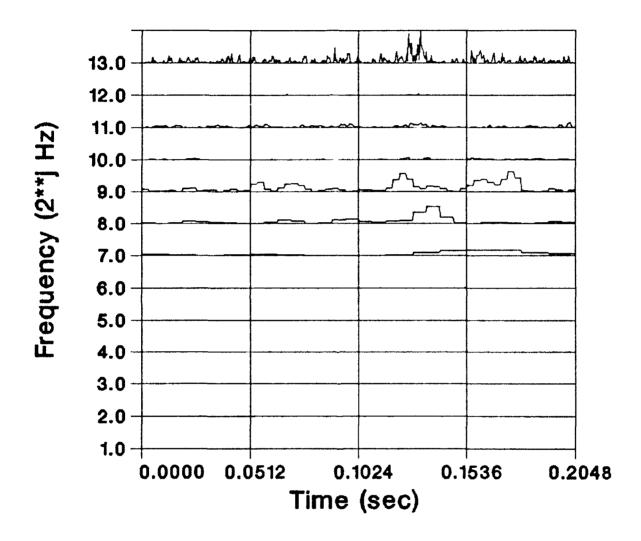


Figure 12. Time patterns of actual pump signal (a) without and (b) with abnormal condition.



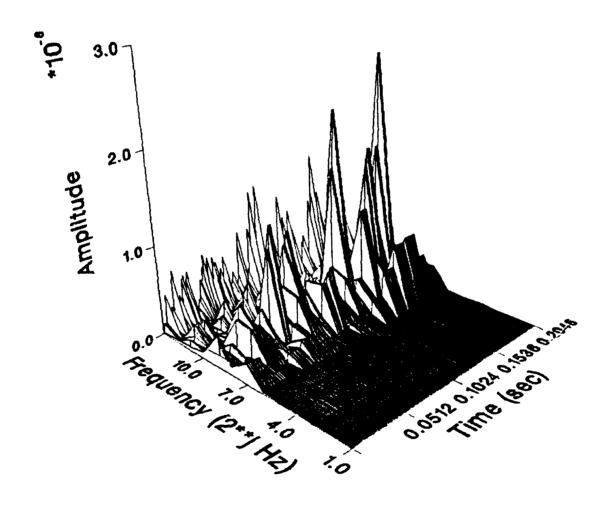
(a)

Fig.13 (continued)



(b)

Figure 13. Time-frequency localization 2-D map of wavelet transform for Fig. 12(a) and (b), respectively ($f_S = 10 \text{ kHz}$, N=2048).



(a)

Fig.14 (continued)

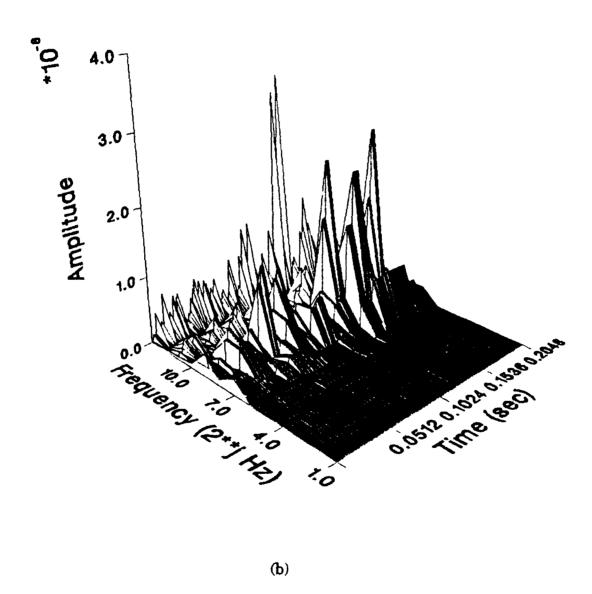
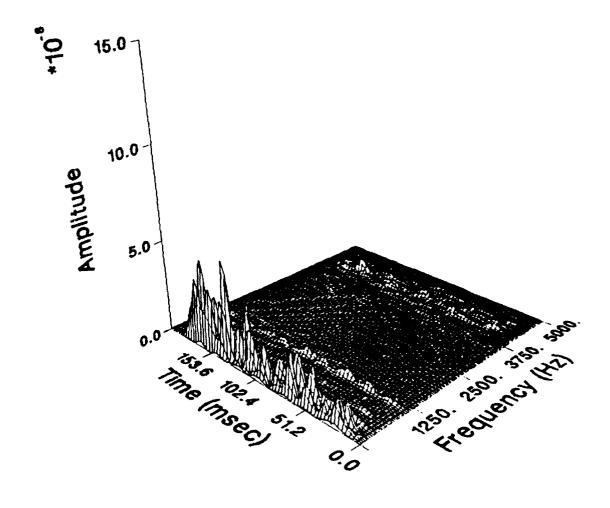


Figure 14. Time-frequency localization 3-D map of wavelet transform for Fig. 12(a) and (b), respectively ($f_S=10 \text{ kHz}$, N=2048).



(a)

Fig.15 (continued)

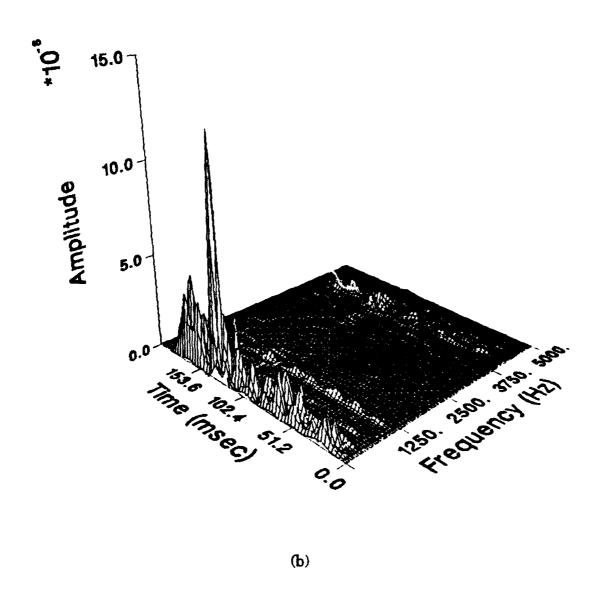


Fig.13 Time-frequency localization of PWVD for Fig. 12(a) and (b), respectively (f_S = 10 kHz, N = 2048).

VI. CONCLUSIONS

The wavelet transform has been investigated and applied to analyzing sampled signal and the actual pump signal. The results of this research will be valuable asset for the analysis of vibration records and condition monitoring of machinery. The following conclusions can be drawn:

- (1) The wavelet transform is ideally suited for portraying the wide-band transient or nonstationary vibration records in time-frequency domain.
- (2) The wavelet transform has a great advantage to detect the small disturbance of the signal.
- (3) The computation time of wavelet transform is very short in comparison with other time-frequency localization techniques.
- (4) The modified Gaussian wavelet was well behavior and very effective to analyze the vibration records.
- (5) The wavelet transform characterizes the time-frequency localization of the signal well and may be useful tool for the machinery condition monitoring.
- (6) If the wavelet level, that is, frequency band, is selected at wavelet transform, its results will be a useful tool for the effective pattern recognition of machinery diagnosis and monitoring.

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APPENDIX. PROGRAM LIST

A. Program List of Wavelet Transform(FORTRAN 77)

С					
	pro	gram wavelet			
C					
c					
C					
C		WAVELET TRANSFORM			
C					
C		by			
C					
C		Dept. of Mechanical Engineering			
C		Naval Postgraduate School			
C					
c					
C					
C		This program is a wavelet transform by using modified			
c	Gau	issian wavelet (octave sweep or 1/3 octave sweep).			
C					
C	Var	Variables			
C					
C	n	= number of input data(n must be the power of 2.)			
C	fs	= sampling frequency			
C	dt	= sampling time(time interval)			
C	bw	= cutoff frequency in highpass filter			
C	а	= dilation			
C	b	= translation			
C	w	= coefficient of wavelet transform w(a,b) **2			
c					
c	Arr	ay			
c					
С	x(i)	= input data set			

```
x1(i) = filtered input data set
C
      bk(i) = filter weight
C
C
      dimension x(8192),bk(4100),x1(8192)
      complex ai,sum
      character*16 inname,outname
      character as
C
      ai=cmplx(0.,1.)
      pi=atan(1.)*4.
C
      print*
      print*,
                       WAVELET TRANSFORM'
      print*
      print*
      print*,'What is an input filename?'
      read(*,10) inname
      print*, What is an output filename?'
      read(*.10) outname
      format(a16)
10
C
      select the sweep method
C
C
      print*, What do you want the sweep method?'
      print*,' if 1/1 octave, input 1'
      print*,' if 1/3 octave, input 2'
      read(*,*) mswp
C
      read the input data file
C
C
      call indata(inname,x,fs,n,nn)
C
```

```
dt=1./fs
C
        call smean(n,x)
C
        print*,'Do you want to apply highpass digital'
        print*, 'filter to the original data? (y/n)'
        read(*,20) as
        format(a1)
20
        if (as.eq.'Y'.or.as.eq.'y') then
             print*, Enter the cutoff frequency of
             print*,'the digital highpass filter (in Hz)'
             read(*,*) bw
        endif
C
        signal modifications
c
C
        Application of highpass digital filter
C
C
        if (as.eq.'Y'.or.as.eq.'y') then
             mo=n/2
        calculate the filter weighting
C
        call filter(mo,bw,dt,bk)
        write(*,*) 'finished filtering'
        pass the highpass filter
        do 160 i=1,n
160
        x1(i)=0.
        do 200 i=1,n
             do 170 k=-mo,mo
```

j=k

```
if (k.lt.0) then
                          j=k*(-1)
                   endif
                   j=j+1
                   ll=i-k
                   if (ll.lt.1) then
                          ll=ll+n
                   elseif (ll.gt.n) then
                          ll=ll-n
                   endif
                   bb=-bk(j)
                   if (k.eq.0) then
                          bb=1-bk(j)
                   endif
                   x1(i)=x1(i)+bb*x(ll)
170
             continue
200
        continue
        do 210 i=1,n
             x(i)=x1(i)
210
        endif
        if (mswp.eq.1) then
            nk=nn
            fac=1.
        elseif (mswp.eq.2) then
             nk=3*nn
             fac=3.
        endif
        nr=nk-int(fac)+1
        open(7,file=outname,status='new')
C
        calculate wavelet transform
C
C
        tini=0.
```

```
ttime=dt*n
f0=2.*pi
write(7,*) tini
write(7,*) ttime
write(7,*) nn,index
do 1000 i=1,nr
    fio=2**((nk-i+1)/fac)
    a=fio*dt
    nm=int(ttime/a)
    if (nm.eq.0) nm=1
    ddt=ttime/nm
    sr=sqrt(-alog(0.01)*2)*fio
    max=int(sr)
    if (max.ge.2*n) max=2*n
    do 900 j=1,nm
           sum=cmplx(0.,0.)
           b=ddt/2.+ddt*float(j-1)
           jk=int(b/dt)+1
           do 800 k=-max,max
                 t=k*dt/a
                 k1=jk+k
                 if (k1.lt.1) then
                       if (k1.lt.-n) then
                             k1=k1+2*n
                       else
                             k1=k1+n
                       endif
                 endif
                 if (k1.gt.n) then
                       if (k1.ge.2*n) then
                             k1=k1-2*n
```

```
endif
                        sum=sum+x(k1)*cexp(-ai*f0*t)*exp(-t*t/2.)*dt
                  continue
800
                  w=cabs(sum)/sqrt(a)
                  w=abs(w)*abs(w)
                  write(7,*) i,j,w
900
            continue
1000
       continue
       close(7)
       stop
       end
C
C
       SUBROUTINES
       subroutine indata(inname,x,fs,n,nn)
       dimension x(*)
       character*16 inname
C
       open(5,file=inname,status='old')
       read(5,*) fs,n
       do 100 j=1,n
            read(5,*) t,x(j)
100
       continue
       close(5)
       ft=fs/2.
       do i=1,20
```

else

endif

k1=k1-n

```
ii=2**i
            di=float(ii)
            if (di.ge.ft) then
                  nn=i
                  go to 200
            endif
        end do
200
        continue
       return
        end
C
C
       subroutine smean(n,x)
C
        This subroutine calculates and removes the mean value of
C
       the sampled data.
C
Ç
       dimension x(*)
       real meany
C
        asum=0.
       do 100 i=1,n
            asum=asum+x(i)
100
       continue
       meanv=asum/n
       do 200 i=1,n
            x(i)=x(i)-meanv
200
       continue
       return
       end
C
¢
       subroutine filter(mo,b,t,bk)
C
       Routine generates FIR filter weights.
C
```

```
Method devised by Potter, Bickford and Glaze.
C
        There are a total of 2M+1 weights...filter generates M+1.
C
C
        --- variables ---
C
        t = the sampling interval in second.
C
        b = cutoff(half-power point) of the filter in Hz;
C
              must be on the range from o to 1/2t.
C
C
        Results are stored in bk
C
C
   ---- Note; in the case of highpass filter, the value of
              weight b0 must use 1-b0 instead of b0.
C
C
        dimension bk(*),d(3)
        data d0/0.35577019/,d(1)/0.2436983/,d(2)/0.07211497/,
       * d(3)/0.00630165/
        pi=atan(1.)*4.
        m=m_0
        first generate plain boxcar weights
C
        fact=2.*b*t
        bk(1)=fact
        fact=fact*pi
        do 5 i=1,m
        fi=i
        bk(i+1)=sin(fact*fi)/(pi*fi)
5
        trapezoidal weighting at end
C
        bk(m+1)=bk(m+1)/2.
        Now apply the Potter p310 window
C
        sumg=bk(1)
        do 15 i=1,m
        sum=d0
        fact=pi*float(i)/float(m)
           do 10 k=1,3
10
                sum=sum+2.*d(k)*cos(fact*float(k))
        bk(i+1)=bk(i+1)*sum
        sumg = sumg + 2.*bk(i+1)
15
```

m1=m+1
do 20 i=1,m1
20 bk(i)=bk(i)/sumg
return
end

B. Program List of wavelet transform(MATLAB)

```
%
                  Wavelet Transform
%
%
%
                         by
%
            Dept. of Mechanical Engineering
               Naval Postgraduate School
%
%
%
                  Ver. 1.0
                              Aug. 5 1993
%
%
                  By using MATLAB Ver. 4.0
%
%
        -- Variables
            infile = input filename
%
            fs
%
                  = sampling frequency
                  = the number of sampled dat
%
            n
%
                     (n must be n-th power of 2.)
                  = mean value of sampled data
%
            avg
            fact = the factor of sweep rate
%
            x(i) = the magnitude of signal
%
%
            z(i,j) = the result of wavelet transform
%
       load c:\users\infile
       fs=infile(1,1);
       n=infile(1,2);
       dt=1/fs;
       x=infile(2:n+1,2);
       asum=0;
%
       remove mean value
%
%
       for j1=1:n
            asum=asum+x(j1);
       end
```

```
avg=asum/n;
       for i1=1:n
            x(i1)=x(i1)-avg;
       end
%
%
       Decide the sweep rate
%
       fact=input('sweep method: 1/1 octave =1, 1/3 octave = 3 ');
%
       ft=fs/2;
       for i1=1:20
            ii=2^i1;
            if ii >= ft
               nn=i1;
               break
            end
       end
       if fact == 1
            nk=nn;
       else
            nk=fact*nn;
       end
       nr=nk-fix(fact)+1;
%
       calculate wavelet transform
%
%
       tini=0;
       ttime=n*dt;
       f0=2*pi;
       jm=fix(ttime/(2*dt));
       wt=zeros(nr,jm);
       for i1=1:nr
          io=2^((nk-i1+1)/fact);
          a=io*dt;
           nm=fix(ttime/a);
```

```
if nm == 0
   nm = 1;
end
ddt=ttime/nm;
sr=sqrt(-log(0.01)*2)*io;
mx=fix(sr);
if mx >= (2*n)
  mx=2*n;
end
for j=1:nm
  sum=0+i*0;
  b=ddt/2+ddt*(j-1);
  jk=fix(b/dt)+1;
  for k=-mx:mx
     t=k*dt/a;
     k1=jk+k;
     if k1 < 1
         if k1 < -n
            k1=k1+2*n;
         else
            k1=k1+n;
         end
     end
     if k1 > n
        if k1 >= 2*n
            k1=k1-2*n;
        else
            k1=k1-n;
        end
     end
     x1=0.-i*f0*t;
     sum=sum+x(k1)*exp(x1)*exp(-t*t/2)*dt;
  end
  w=abs(sum)/sqrt(a);
  w=abs(w)*abs(w);
```

```
wt(i1,j)=ww;
Plotting
line=128;
z=zeros(nr,line);
for i1=1:nr
   io=2^{(nk-i+1)/fact)};
   a=io*dt;
   k=fix(ttime/a);
   if k == 0
     k=1:
   end
   if k <= line
     step=line/k;
     k2=0;
     for ii=1:k
        k1=k2+1;
        k2=fix(step*ii);
        st=k2-k1+1;
        if st <= step
            cf=step/st;
        else
            cf=st/step;
        end
        for ij=k1:k2
            z(i1,ij)=wt(i1,ii)/cf/st;
        end
     end
   else
     step=k/line;
     k2=0;
     for ii=1:line
        k1=k2+1;
        k2=fix(step*ii);
```

%

% %

```
st=k2-k1+1;
        ssum=0;
        for ij=k1:k2
           ssum=ssum+wt(i1,ij);
        end
       if st <= step
           ssum=ssum*step/st;
        else
           ssum=ssum*st/step;
        end
        z(i1,ii)=ssum;
     end
  end
end
xma=max(z);
xp=max(xma)*1.2;
dt1=ttime/(line-1);
for k=1:line
   xvalue=(k-1)*dt1;
   xx(k)=xvalue;
end
for k=1:nr
  yy(k)=k;
end
surf(xx,yy,z)
xlabel('Time (sec)')
ylabel('Frequency step ')
zlabel('Amplitude')
axis([tini ttime 1 nr 0 xp])
```

C. Plotting Program List (3 Dimension)

- FOTRAN 77 and CA-DISSPLA Graphic Package -

```
C
       program plot
C
       This program uses the graphic package CA-DISSPLA to
C
       plot the results of wavelet transform
C
C
       tmax
                  = time record length
C
       tint
                  = initial time
C
       fmin
                  = start frequency step
C
       fmax
                  = stop frequency step
C
                  = the number of the frequency step
       nn
C
       fac
                  = index of sweep method
C
       fname
                  = input data filename generated by main source
C
                    program
C
C
       dimension rr(32768), wt(50,256)
       character*25 fname
C
       write(*,*) 'input file name?'
       read(*,20) fname
       format(a25)
20
C
       data distribution or reduction for 3-D graphics
C
C
       line=256
       open(8,file=fname,status='old')
       read(8,*) tini
       read(8,*) tmax
       read(8,*) nn,n,fac
       nk=nn*int(fac)
       nr=nk-int(fac)+1
```

```
ddt=tmax/n
do 1000 i=1,nr
    fio=2.**((nk-i+1)/fac)
     a=fio*ddt
k=int(tmax/a)
if (k.eq.0) k=1
if (k.le.line) then
    step=float(line)/float(k)
     k2=0
    do 950 ii=1,k
         read(8,*) i1,j1,w
        k1=k2+1
         k2=int(step*ii)
         st=float(k2-k1)+1.
         if (st.le.step) then
           coe=step/st
         else
           coe=st/step
         endif
         do 930 ij=k1,k2
           wt(i,ij)=w/coe/st
         continue
     continue
else
    step=float(k)/float(line)
     k2=0
    do 800 ii=1,line
        k1=k2+1
        k2=int(step*ii)
        sum=0.
        st=float(k2-k1)+1.
        do 750 ij=k1,k2
           read(8,*) i1,j1,w
           sum=sum+w
        continue
```

930

950

750

```
if (st.le.step) then
                  sum=sum*step/st
               else
                  sum=sum*st/step
               endif
               wt(i,ii)=sum
800
            continue
          endif
1000
        continue
        close(8)
        smax=0.
       do 2000 i=1,nr
          do 2000 j=1,line
            if (smax.le.wt(i,j)) smax=wt(i,j)
       continue
2000
       write(*,*) 'maximum=',smax
       write(*,*) 'input the maximum scale ?'
       read(*,*) fact
        do 120 i=1,nr
           do 100 j=1,line
            k=line*(i-1)+j
            rr(k)=wt(i,j)
100
           continue
120
        conunue
        dd=mod(nr,2)
       if (dd.eq.0) then
           nr=nr+1
           kk=(nr-1)*line+1
           kl=nr*line
           do 150 ip=kk,kl
            rr(ip)=0.
150
        endif
```

```
plotting
call pdev('ln03',ieer)
call hwshd
call swissm
call shdchr(90.,1,0.002,1)
call height(0.15)
call physor(1.1,1.2)
call area2d(5.5,6.75)
call messag('WAVELET TRANSFORM $',100,1.1,8.2)
call blsur
call volm3d(8.,8.,9.)
call x3name('Time (sec) $', 100)
call y3name('Frequency step', 100)
call z3name('Amplitude $', 100)
call zaxang(90.)
fmax=float(nr)
fstep=(fmax-1)/4.
call graf3d(tini,tmax/4.,tmax,1.,fstep,fmax,0.,'SCALE',fact)
call surmat(rr,1,line,1,nr,1)
call end3gr(0)
call endpl(0)
call donepl
end
```

C

c c

D. Plotting Program List (2 Dimension)

- FOTRAN 77 and CA-DISSPLA Graphic Package -

```
C
       program levelplot
C
       This program uses the graphic package CA-DISSPLA to
C
       plot the results of wavelet transform with respect to each level.
C
C
       tmax
                  = time record length
       tint
                  = initial time
C
                  = start frequency step
       fmin
C
       fmax
                  = stop frequency step
       nn
                  = the number of the frequency step
C
       fac
                  = index of sweep method
C
                  = input data filename generated by main source
       inname
C
                     program
C
C
       dimension x(512),y(512),wt(50,256)
       character*25 inname
C
       write(*,*) 'input file name ?'
       read(*.20) inname
       format(a25)
20
C
       data distribution or reduction for 2-D graphics
C
C
       line=512
       open(8,file=fname,status='old')
       read(8,*) tini
       read(8,*) tmax
       read(8,*) nn,n,fac
       nk=nn*int(fac)
       nr=nk-int(fac)+1
       ddt=tmax/n
```

```
do 1000 i=1,nr
              fio=2.**((nk-i+1)/fac)
              a=fio*ddt
              k=int(tmax/a)
              if (k.eq.0) k=1
              if (k.le.line) then
                  step=float(line)/float(k)
                 k2=0
                  do 950 ii=1,k
                    read(8,*) i1,j1,w
                    k1=k2+1
                    k2=int(step*ii)
                    st=float(k2-k1)+1.
                    if (st.le.step) then
                       coe=step/st
                    else
                       coe=st/step
                    endif
                    do 930 ij=k1,k2
                       wt(i,ij)=w/coe/st
930
                    continue
950
                continue
             else
                step=float(k)/float(line)
                k2=0
                do 800 ii=1,line
                    k1=k2+1
                   k2=int(step*ii)
                    sum=0.
                   st=float(k2-k1)+1.
                   do 750 ij=k1,k2
                       read(8,*) i1,j1,w
                       sum=sum+w
750
                   continue
                   if (st.le.step) then
                       sum=sum*step/st
```

```
else
                   sum=sum*st/step
               endif
               wt(i,ii)=sum
800
             continue
          endif
        continue
1000
        close(8)
        smax=0.
        do 2000 i=1.nr
          do 2000 j=1,line
            if (smax.le.wt(i,j)) smax=wt(i,j)
2000
        continue
        write(*,*) 'maximum=',smax
        write(*,*) 'input the maximum scale ?'
        read(*,*) smax
C
         normalizing
C
C
        do 2500 i=1,nr
           do 2500 j=i,line
              wt(i,j)=wt(i,j)/smax
2500
C
        plotting
C
C
        call pdev('ln03',ieer)
        call hwshd
        call swissm
        call shdchr(90.,1,0.002,1)
        call height(0.15)
         call page(8.5,11.)
        call physor(1.5,1.5)
        call area2d(4.8,4.7)
```

```
call xname('Time (sec) $', 100)
        call yname('Frequency step', 100)
        call headin('WAVELET TRANSFORM $',100,1.1,1)
        call thkfrm(0.01)
        call yaxang(0.)
        call graf(tini,tmax/4.,tmax,1.,1.,nr+1)
        call grid(1,1)
        do 3000 i=1,nr
           do 2700 j=1,line
             x(j)=dt*float(j)
             y(j)=float(i)+wt(i,j)
2700
           continue
        call curve(x,y,line,0)
3000
        continue
        call endpl(0)
       call donepl
       stop
       end
```

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